### The Nature of the Chemical Bond Revisited: An Energy-Partitioning Analysis of Nonpolar Bonds

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Abstract: The nature of the chemical bond in nonpolar molecules has been investigated by energy-partitioning analysis (EPA) of the ADF program using DFT calculations. The EPA divides the bonding interactions into three major components, that is, the repulsive Pauli term, quasiclassical electrostatic interactions, and orbital interactions. The electrostatic and orbital terms are used to define the nature of the chemical bond. It is shown that nonpolar bonds between main-group elements of the first and higher octal rows of the periodic system, which are prototypical covalent bonds, have large attractive contributions from classical electrostatic interactions, which may even be stronger than the attractive orbital interactions. Fragments of molecules with totally symmetrical electrondensity distributions, like the nitrogen atoms in  $N_2$ , may strongly attract each other through classical electrostatic forces, which constitute 30.0% of the total attractive interactions. The electrostatic attraction can be enhanced by anisotropic charge distribution of the valence electrons of the atoms that have local areas of (negative) charge concentration. It is shown that the use of atomic partial charges in the analysis of the nature of the interatomic interactions may be misleading because they do not reveal the topography of the electronic charge distribution. Besides dinitrogen, four groups of molecules have been studied. The attractive binding interactions in  $H<sub>n</sub>E-EH<sub>n</sub>$  (E= Li to F;  $n=0-3$ ) have between 20.7  $(E=F)$  and 58.4%  $(E=Be)$  electrostatic character. The substitution of hydrogen by fluorine does not lead to significant changes in the nature of the binding interactions in  $F<sub>n</sub>E-EF<sub>n</sub>$  (E= Be to O). The electrostatic contributions to the attractive interactions in  $F<sub>n</sub>E-EF<sub>n</sub>$  are between 29.8 (E=O) and 55.3% ( $E = Be$ ). The fluorine substituents have a significant effect on the Pauli repulsion in the nitrogen and oxygen compounds. This explains why  $F_2N-NF_2$  has a much weaker bond than  $H_2N-NH_2$ , whereas the interac-

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tion energy in FO-OF is much stronger than in HO-OH. The orbital interactions make larger contributions to the double bonds in  $HB=BH$ ,  $H_2C=$  $CH<sub>2</sub>$ , and HN=NH (between 59.9% in  $B_2H_2$  and 65.4% in  $N_2H_2$ ) than to the corresponding single bonds in  $H<sub>n</sub>E-$ EH<sub>n</sub>. The orbital term  $\Delta E_{\rm orb}$  (72.4%) makes an even greater contribution to the  $HC=CH$  triple bond. The contribution of  $\Delta E_{\text{orb}}$  to the H<sub>n</sub>E=EH<sub>n</sub> bond increases and the relative contribution of the  $\pi$  bonding decreases as E becomes more electronegative. The  $\pi$ -bonding interactions in HC=CH amount to 44.4% of the total orbital interactions. The interaction energy in  $H_3E-EH_3$  $(E=C$  to Pb) decreases monotonically as the element E becomes heavier. The electrostatic contributions to the  $E-E$ bond increases from  $E=C(41.4\%)$  to  $E = Sn$  (55.1%) but then decreases when  $E = Pb$  (51.7%). A true understanding of the strength and trends of the chemical bonds can only be achieved when the Pauli repulsion is considered. In an absolute sense the repulsive  $\Delta E_{\text{Pauli}}$  term is in most cases the largest term in the EPA.

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#### Introduction

According to the classical view of chemical bonding, nonpolar bonds between identical fragments  $R$  in a molecule  $R-R$ are established through covalent interactions. The model of a covalent bond consisting of a pair of electrons shared between two atoms was introduced into chemistry by Lewis.<sup>[1,2]</sup> This type of chemical bonding, which leads in most cases to an accumulation of the interatomic electronic charge, $[3]$  is conceptually different from ionic bonding which can be described in terms of the classical Coulombic attraction that arises when two charges of opposite sign attract each other. In modern terminology, covalent bonding is a result of interactions between shared electrons while ionic bonding arises from closed-shell interactions between separated fragments which carry opposite charges, that is, charged species whose electron densities do not overlap. Ionic bonding can be described by the laws of classical electrostatic interactions.

The understanding of covalent bonds in terms of the basic laws of physics puzzled scientists for a long time until quantum theory was developed and applied to chemical problems. Heitler and London showed in 1927 that the strongly attractive forces between two hydrogen atoms can only be understood when the electrons are described as wave functions, which are then used to express the electronic structure of  $H_2$ <sup>[4]</sup> Heitler and London called it a "characteristic quantum mechanical resonance phenomenon", which is crucial for the understanding of the interactions between neutral atoms. It should be emphasized that covalent and ionic bonding are both the result of electrostatic forces. We would also like to point out that besides the electrostatic interactions the kinetic energy of the electrons is also very important for the chemical bond.<sup>[5]</sup> The difference is that quantum theoretical laws enforce electrons to behave in a peculiar way when they interact, which can be understood by treating them as resonating waves which may lead to a strong attraction that yields chemical bonding. We would like to point out that the "resonance phenomenon", known as orbital interactions in modern terminology, is not associated with the pairing of two electrons which Lewis believed to be the driving force for a covalent bond. Resonance of the wave function takes place when there is only one electron such as in  $H_2$ <sup>+</sup>.<sup>[6]</sup>

Calculation of the quasiclassical $[7]$  electrostatic interactions,  $\Delta E_{\text{elstat}}$ , between two hydrogen atoms at the equilibrium distance of  $H<sub>2</sub>$  (a so-called promolecule) indicates only a spurious attraction. Nearly all the bonding energy in dihydrogen comes from the resonating wave function. Since the wave function is usually described in terms of one-electron functions called molecular orbitals, the bonding in  $H_2$  arises nearly exclusively from orbital interactions. This finding has led covalent interactions in nonpolar bonds to be described in many chemistry textbooks only in terms of molecular orbitals, that is, covalent bonding and orbital interactions are considered as synonymous. Polar bonds between different atoms or groups  $R-R'$  are then considered to have contributions from both covalent and ionic attractions. However, a

value of  $\Delta E_{\text{elstat}}$ ~0 for H<sub>2</sub> is atypical of nonpolar diatomic molecules! In 1986 Spackman and Maslen calculated the electrostatic energies of 148 polar and nonpolar diatomic compounds.[8] They showed that the quasiclassical electrostatic attraction in 18 homoatomic species  $E_2$ , where E is an element up to the fourth row of the periodic table, is always very large except for H<sub>2</sub>. The calculated values of  $\Delta E_{\text{elstat}}$ were in most cases even larger than the bond dissociation energies ! For example, the quasiclassical electrostatic attraction between two spherical nitrogen atoms in the <sup>4</sup>S ground state at the equilibrium distance of  $N_2$  was calculated to be  $\Delta E_{\text{elstat}} = -330.7 \text{ kcal mol}^{-1[8]}$  while the bond dissociation energy (BDE) of dinitrogen is 228.5 kcalmol<sup>-1</sup>.<sup>[9]</sup> This is in striking contrast to  $H_2$  which has a BDE of 109.6 kcal mol<sup>-1[9]</sup> but the calculated value for  $\Delta E_{\text{elstat}}$  is only  $-1.4$  kcalmol<sup>-1</sup>.<sup>[8]</sup>

Spackman and Maslen were not the first to recognize that the quasiclassical Coulombic attraction in diatomic molecules  $E_2$  is very large when E is not hydrogen. Hirshfeld and Rzotkiewicz reported as early as 1974 that the net electrostatic attraction makes a much larger contribution to the bonding of the heavier first-row  $E_2$  molecules than to the bonding in  $H_2$ <sup>[10]</sup> The unusually weak electrostatic attraction in  $H<sub>2</sub>$  is a consequence of its small nuclear charge and the shape of the electronic charge cloud. The larger positive charge of the heavier nuclei results in a strong electrostatic attraction for the electrons of other neutral atoms at intermediate internuclear distances, which is contrary to the general belief that there are only weak electrostatic interactions between neutral atoms at equilibrium distance.

Several workers have pointed out that the quasiclassical electrostatic attraction in heavier nonpolar molecules is quite strong,<sup>[6,11,12a]</sup> but this knowledge has not led to a change in the standard interpretation of the nature of the interatomic interactions in nonpolar bonds that is found in many chemistry textbooks. Very recently, Rioux carried out a survey of popular general chemistry textbooks and showed that none of them gives an accurate description of covalent bonding.<sup>[13]</sup> In particular, the kinetic energy of the electrons, which plays a paradoxical role in the formation of the chemical bond, as shown by the pioneering work of Ruedenberg,<sup>[14]</sup> is never mentioned. Furthermore, the role of electrostatic interactions is described incorrectly.

There are several reasons why the knowledge about the physical origin of the chemical bond that has been gained in recent decades<sup>[6]</sup> has had little impact on the way covalent bonding is presented and explained in chemistry textbooks. One reason is that Lewis' bonding model, $[1]$  which received quantum-chemical brute-force support from Pauling,<sup>[15]</sup> is deceptively easy to interpret in terms of classical electrostatic interactions. Many chemists have a strong tendency to judge the value of a bonding model more by its simplicity and ease of visualization than by its agreement with physical laws and quantum theoretical insights. This can be explained by consideration of the early attempts to rationalize chemical bonding prior to the advent of quantum theory, when a true understanding of the chemical bond based on the first

principles of physics was not possible. The heuristic models that were developed during this time were remarkably successful; not only were they used to rationalize experimental observations, they also served as helpful guidelines in the search for new compounds and novel reactions, making them very popular amongst the wider chemical community. The quantum theoretical explanation of chemical bonding, in which the wave function  $\Psi$  was introduced as the fundamental quantity for describing electrons, deterred chemists from accepting a theoretical interpretation of the chemical bond for a long time owing to its complicated mathematical derivation and, more importantly, because the results are difficult to cast into simple models. Although quantum theory quickly proved invaluable for understanding chemical bonding, for example, it allowed longstanding problems such as the triplet ground state of dioxygen<sup>[16a]</sup> and the peculiar stability of aromatic compounds<sup>[16b]</sup> to be solved, it was treated like an illegitimate child by orthodox chemistry practitioners for a long time. Organic chemists eventually accepted the wave function as a helpful quantity because pericyclic reactions could only be explained by MO arguments by using the symmetry of  $\Psi$ . The didactical approach and the use of simple figures, which were introduced by Woodward and Hoffmann in their ground-breaking work, were important reasons for the acceptance of the wave function.[17]

This does not mean that we think it necessary to discard the heuristic bonding models that are so widely used in chemistry. What is required, however, is an interpretation of the models that is in agreement with the physical origin of the chemical bond. It is necessary to connect the historically derived bonding models with the knowledge of the interatomic interactions that has been gained through accurate quantum theoretical investigations. Quantum theoretical support for an empirical chemical heuristic model is important for two reasons: one learns where the limits of the model are to be expected and how the model can be extended so it is more reliable. With this paper we wish to contribute to this endeavour. The goal of this study was to quantitatively interpret the chemical bond in terms of quasiclassical electrostatic interactions, the Pauli repulsion, and orbital interactions through accurate quantum-chemical calculations. The relative strengths of the attractive contributions to chemical bonding, that is, the electrostatic,  $\Delta E_{\text{elstat}}$ , and orbital,  $\Delta E_{\rm orb}$ , interactions, can then be used to classify and to compare chemical bonds.

Before starting, we wish to comment on the terms "ionic bonding" and "electrostatic interactions" to avoid confusion. The former term describes the attractive interactions between two ions that have opposite charges, which can be understood in terms of the classical electrostatic attraction between a positive and a negative charge. Thus, ionic bonding as it is found in ionic solids is largely the result of purely electrostatic interactions. However, electrostatic interactions do not automatically mean that there is ionic bonding. Nonpolar (covalent) bonds may also contain strong electrostatic attractions between the bonded atoms which can make a larger contribution to the bonding than the orbital interactions. The change in the absolute and relative contributions of the orbital and electrostatic attractions on going from nonpolar to polar bonds is the topic of another paper.<sup>[18]</sup>

In this paper we will first present the results of the bonding analysis of  $N_2$ . The calculated value for the electrostatic attraction,  $\Delta E_{\text{elstat}}$ , will be compared with the result reported by Spackman and Maslen.<sup>[8]</sup> Spackman and Maslen write in their paper "A more detailed analysis of bonding in diatomics, in the spirit of that outlined by Morokuma and Kitaura, may well be warranted." This is exactly what we report in this paper, although our analysis, however, extends beyond diatomic molecules. We have used the energy-partitioning analysis (EPA) of the ADF program, $[12]$  which is based on the methods of Morokuma<sup>[19]</sup> and Ziegler and Rauk.<sup>[20]</sup> After discussing the bonding analysis of  $N_2$  we analyze the homolytic bonding between singly bonded elements of the first octal row of the periodic table  $H_nE-EH_n$  (E=Li to F), that is, of the nonpolar molecules  $Li<sub>2</sub>$ , HBe-BeH,  $H<sub>2</sub>B-BH<sub>2</sub>$ ,  $H_3C$ –CH<sub>3</sub>, H<sub>2</sub>N–NH<sub>2</sub>, HO–OH, and F<sub>2</sub>. We also investigate the changes in the nature of the  $E-E$  bonds when hydrogen is substituted by fluorine, that is, in the molecules  $F<sub>n</sub>E-EF<sub>n</sub>$  $(E=Be$  to O). In the third part we analyze the bonding interactions in the multiple bonds HB=BH,  $H_2C=CH_2$ , HC= CH, and HN=NH. In the final part of the study the  $H_3C$  $CH<sub>3</sub>$  bond in ethane is compared with the  $H<sub>3</sub>E-EH<sub>3</sub>$  bond of the heavier Group 14 elements  $(E = Si$  to Pb). The results suggest that the standard interpretation of nonpolar bonds, which considers only orbital interactions, should be modified. In addition to the Pauli repulsion, there are two attractive components, the orbital and quasiclassical electrostatic interactions, that contribute to the total interaction energy. The use of Kohn–Sham orbitals instead of Hartree–Fock orbitals has been justified by Baerends and co-workers.<sup>[12,21]</sup>

This paper is a continuation of our systematic studies of the nature of the chemical bond. In previous studies we focussed on the bonding in donor–acceptor complexes, that is, the bonding interactions that take place between closedshell fragments.<sup>[22]</sup> We are presently studying the bonding interactions between open-shell fragments. We wish to point out that there are other workers in the field who have recently reported energy-partitioning analyses of chemical bonds.[23]

#### Methods

The geometries of the molecules were optimized at the nonlocal DFT level of theory by using Becke's exchange functional<sup>[24a]</sup> in conjunction with Perdew's correlation functional<sup>[24b]</sup> (BP86). Uncontracted Slater-type orbitals (STOs) were employed as basis functions in SCF calculations.[25a] Triple- $\xi$ -quality basis sets were used, which were augmented by two sets of polarization functions, that is, p and d functions for the hydrogen atom and d and f functions for the other atoms. This level of theory is denoted as BP86/TZ2P. An auxiliary set of s, p, d, f, and g STOs was used to fit the molecular densities and to represent the Coulomb and exchange potentials accurately in each SCF cycle.<sup>[25b]</sup> Scalar relativistic effects were considered by using the zero-order regular approximation (ZORA).<sup>[26]</sup> All structures were verified as minima on the potential energy surface by

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calculating the Hessian matrices. The atomic partial charges were calculated by using the Hirshfeld partitioning scheme.<sup>[27]</sup> The calculations were carried out using the ADF(2.3) program package.<sup>[12]</sup>

The N $\equiv$ N, H<sub>n</sub>E-EH<sub>n</sub>, and F<sub>n</sub>E-EF<sub>n</sub> binding interactions were analyzed by using the ADF energy-partitioning scheme<sup>[12]</sup> which was originally developed by Morokuma<sup>[19]</sup> and later modified by Ziegler and Rauk.<sup>[20]</sup> The focus of the bonding analysis was the instantaneous interaction energy,  $\Delta E_{\text{int}}$ , of the bond, which is the energy difference between the molecule and its fragments in the frozen geometry of the compound. The interaction energy can be divided into three main components [Eq. (1)],

$$
\Delta E_{\text{int}} = \Delta E_{\text{elstat}} + \Delta E_{\text{Pauli}} + \Delta E_{\text{orb}} \tag{1}
$$

where  $\Delta E_{\text{elstat}}$  is the electrostatic interaction energy between the fragments and is calculated by using the frozen electron-density distribution of the N,  $EH_n$  or  $EF_n$  fragments in the N=N,  $H_nE-EH_n$  or  $F_nE-EF_n$  molecules. The second term in Equation (1),  $\Delta E_{\text{Pauli}}$ , refers to the repulsive interactions between the fragments, which are caused by the fact that two electrons with the same spin cannot occupy the same region in space.  $\Delta E_{\text{Pauli}}$  is calculated by enforcing the Kohn–Sham determinant of the orbitals of the superimposed fragments to obey the Pauli principle by antisymmetrization and renormalization. The stabilizing orbital interaction term,  $\Delta E_{\rm orb}$ , which incorporates the Heitler–London resonance phenomenon $\mathbb{R}^{4}$  and has additional contributions from polarization and relaxation. is calculated in the final step of the energy-partitioning analysis when the Kohn–Sham orbitals relax to their optimal form. This term can be further partitioned into contributions from the orbitals that belong to different irreducible representations of the point group of the interacting system. The interaction energy,  $\Delta E_{\text{int}}$ , together with the term  $\Delta E_{\text{prep}}$ , which is the energy necessary to promote the fragments from their equilibrium geometry to the geometry in the compounds, can be used to calculate the bond dissociation energy,  $D_e$ , [Eq. (2)].<sup>[28]</sup> Further details of the energypartitioning analysis can be found in the literature.<sup>[12]</sup>

$$
-D_e = \Delta E_{\text{prep}} + \Delta E_{\text{int}} \tag{2}
$$

It is important to recognize the physical meaning and the relevance of the energy terms involved in the EPA,  $\Delta E_{\text{elstat}}$ ,  $\Delta E_{\text{Pauli}}$ , and  $\Delta E_{\text{orb}}$ , to avoid misinterpretation of the calculated numbers. In particular, we would like to point out that in the calculation of  $\Delta E_{\text{elstat}}$  the electron-density distribution of the fragments is used without consideration of the polarization of the charge distribution that arises in chemical interactions. The polarization is only considered in the final step of the EPA, which means that stabilization due to polarization and relaxation is completely included in the  $\Delta E_{\rm orb}$  term. Thus, the calculated electrostatic interaction energy,  $\Delta E_{\text{elstat}}$ , of the unpolarized fragments is not the same as the total potential energy change of bond formation because the final electron density differs from the electronic density that results from superposition of the two fragment densities. While the  $\Delta E_{\text{elstat}}$  term contains only quasiclassical electrostatic interactions that arise from the frozen electron densities of the fragments, the  $\Delta E_{\rm orb}$  term contains electrostatic attractions that result from quantum interference, potential energy changes due to polarization and relaxation and kinetic energy contributions. The  $\Delta E_{\text{Pauli}}$ term also contains potential energy contributions because electronic charge is moved from the area of overlap of the fragments to nearer the nuclei which actually lowers the energy. The increase in the total energy due to the  $\Delta E_{\text{Pauli}}$  term comes from the kinetic energy of the electrons which is much higher when they are closer to the nuclei. This is why the  $\Delta E_{\text{Pauli}}$  term is sometimes called kinetic repulsion. [12]

EPA has been used in the past mainly for analyzing the interactions between closed-shell species. To the best of our knowledge, the method was extended to electron-pair bonding for the first time by Bickelhaupt et al.<sup>[29]</sup>

#### **Results**

**Dinitrogen bond N=N:** Table 1 gives the results of the energy-partitioning analysis  $(EPA)$  of the nitrogen-nitrogen bond with nitrogen atoms in the  $1s^2 2s^2 2p_x^2 2p_y^2 2p_z^2$  (4S)

Table 1. Energy decomposition analysis<sup>[a]</sup> of the N $\equiv$ N bond in N<sub>2</sub> at the BP86/TZ2P level of theory.

$N_{2}$
$-240.5$
802.4
$-312.9(30.0\%)$
$-730.0(70.0\%)$
$-479.8(65.7%)$
$-250.3(34.3\%)$
1.102 $(1.09768)^{[e]}$
240.5 $(228.5)^{[e]}$
237.1 $(225.0)^{[e]}$

[a] Energy values are given in kcalmol<sup>-1</sup>. [b] The percentage values in parentheses give the contribution to the total attractive interactions  $\Delta E_{\text{elstat}} + \Delta E_{\text{orb}}$ . [c] The percentage values in parentheses give the contribution to the orbital interactions  $\Delta E_{\text{orb}}$ . [d] The experimental values are given in parentheses. [e] Ref. [9].

ground state used as fragments. The calculated bond dissociation energy ( $D_0 = 237.1$  kcalmol<sup>-1</sup>) is in satisfactory agreement with the experimental value  $(D_0=225.0 \text{ kcal mol}^{-1})$ .<sup>[9]</sup> The theoretical bond energy gives, after correction for the ZPE contribution, a value of  $\Delta E_{\text{int}} = -240.5 \text{ kcal mol}^{-1}$  for the interaction energy. Table 1 shows that the calculated quasiclassical electrostatic attraction  $(\Delta E_{\text{elstat}} = -312.9 \text{ kcal})$  $mol^{-1}$ ) is very similar to the value that was calculated by SM  $(\Delta E_{\text{elstat}} = -330.7 \text{ kcal mol}^{-1})$ .<sup>[8]</sup> Thus, our EPA shows that the electrostatic attraction in the  $N_2$  promolecule is larger than the BDE, in agreement with the previous calculation by SM.

Table 1 shows that the quantum theoretical energy contributions of the electrostatic interactions, that is, the Pauli repulsion  $(\Delta E_{\text{Pauli}} = 802.4 \text{ kcal mol}^{-1})$  and the orbital term  $(\Delta E_{orb} = -730.0 \text{ kcal mol}^{-1})$ , have much higher absolute values than the quasiclassical electrostatic attraction. The sum of the attractive orbital and the repulsive Pauli terms is  $+72.4$  kcalmol<sup>-1</sup>, that is, the quantum theoretically defined energies (which include the contribution of the kinetic energy of the electrons) in  $N_2$  have a weakening effect on the electrostatic attraction at the equilibrium distance. This is in contrast to  $H_2$  in which the bonding is exclusively derived from the orbital term,  $\Delta E_{\rm orb}$ . The energy-partitioning analysis of dihydrogen, using the same level of theory as used in this work, gives a repulsive electrostatic contribution of  $\Delta E_{\text{elstat}}$  = 5.8 kcalmol<sup>-1</sup> at the equilibrium distance. The binding in  $H<sub>2</sub>$  is a result of orbital interactions only which give a stabilizing contribution of  $-118.7$  kcalmol<sup>-1</sup>.<sup>[30]</sup>

The large value for the quasiclassical electrostatic attraction in  $N_2$  may come as a surprise to many chemists who assume that the attractive and repulsive interactions between the positively charged nuclei and the negatively charged electrons in dinitrogen, which has an overall charge of zero, should roughly cancel. A model calculation of the quasiclassical attraction in  $N_2$  by Kutzelnigg gave a similar result.[31] A pictorial explanation was given by Bickelhaupt and Baerends.[32] When two atoms approach each other with spherical charge densities, the repulsion between the interpenetrating clouds is weaker than the repulsion between the point charges that are at the center of the charge. This is why the repulsive term between the electronic charges of the two atoms at intermediate distances is smaller than the two attractive terms (the attraction between the electrons of one atom and the nucleus of the other atom) and the repulsion between the nuclei. The net result is an overall charge attraction.

We analyzed the nitrogen–nitrogen interactions at different interatomic distances by using the EPA method. Figure 1 shows the energy curves for  $\Delta E_{\text{int}}$ ,  $\Delta E_{\text{elstat}}$ ,  $\Delta E_{\text{Pauli}}$ , and  $\Delta E_{\rm orb}$  for N-N distances between 0.6 and 1.8 Å. From the calculations it can be predicted that, on the basis of the electrostatic interactions alone, the dinitrogen molecule would have a bond length of ~0.85 Å, with a value for  $\Delta E_{\text{elstat}}$ of  $\sim$  450 kcalmol<sup>-1</sup>! Assuming that the virial theorem holds at this point (the molecular virial theorem for a stationary



Figure 1. Energy contributions of  $\Delta E_{\text{elstat}}$ ,  $\Delta E_{\text{Pauli}}$  and  $\Delta E_{\text{orb}}$  to the total interaction energy  $\Delta E_{\text{int}}$  in N<sub>2</sub> as a function of N-N interatomic distance: a) large scale; b) small scale.

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system reads  $\Delta E = 0.5 \Delta V$  and  $\Delta V = -\Delta T$ , where V is the potential energy and  $T$  is the kinetic energy), the bond dissociation energy would be  $\sim$  225 kcalmol<sup>-1</sup>, which is close to the experimental value ( $D_e = 228.5$  kcalmol<sup>-1</sup>).<sup>[9]</sup> Classical forces would yield nearly the same BDE for  $N_2$  as was calculated by quantum theory, albeit at a significantly shorter bond length. Figure 1 shows that the curves for  $\Delta E_{\text{int}}$  and  $\Delta E_{\text{elstat}}$ cross at a N-N distance of  $\sim$ 1.3 Å. At shorter distances, the repulsive contributions of  $\Delta E_{\text{Pauli}}$  are stronger than those of the attractive  $\Delta E_{\rm orb}$  term, but at longer N-N distances the latter interactions are stronger than the  $\Delta E_{\text{Pauli}}$  term.

The two attractive energy contributions to the nitrogen nitrogen bond are  $\Delta E_{\text{elstat}} = -312.9 \text{ kcal mol}^{-1}$  and  $\Delta E_{\text{orb}} =$  $-730.0$  kcalmol<sup>-1</sup>. We have previously proposed that the ratio of the two attractive energy terms should be used to define the character of the bond in terms of electrostatic and orbital interactions.[22] The calculated numbers suggest that the chemical bond in  $N_2$  has 30.0% electrostatic character while 70.0% comes from orbital interactions. Note that these percentage values are the contribution to the attractive interactions and not to the total interactions. The breakdown of the  $\Delta E_{\rm orb}$  term into orbitals that belong to different irreducible representations of the  $D_{\omega h}$  point group show that the contribution of the  $\sigma$  bond (-479.8 kcalmol<sup>-1</sup>) is much larger than that of the degenerate  $\pi$  bond (-250.3 kcal  $mol<sup>-1</sup>$ ). This is in agreement with the general assessment that  $\sigma$  bonds are stronger than  $\pi$  bonds. However, Kutzelnigg concluded upon theoretical analysis of the overlapping orbitals of the N-N  $\sigma$  bond that the latter is already in the antibonding region.[33] This is because the interatomic distance is very short. It was suggested that the  $\sigma$  bond is much weaker than the  $\pi$  bond,<sup>[34]</sup> but this seems to be at variance with the values for  $\Delta E_{\sigma}$  and  $\Delta E_{\pi}$  determined by EPA, which are given in Table 1. However, these values refer only to the attractive interactions between electrons with opposite spins, while the repulsive interactions between electrons with the same spin are given by the  $\Delta E_{\text{Pauli}}$  term. The latter cannot be divided into orbitals that have different symmetry but a comparison of the  $\Delta E_{\text{Pauli}}$  value for N<sub>2</sub> (802.4 kcal mol<sup>-1</sup>) with the much smaller value for  $C_2$  (252.3 kcalmol<sup>-1</sup>) suggests that the strong repulsion arises mainly from the electrons in the  $\sigma$  orbitals. Note that the 5s(HOMO) of N<sub>2</sub> is the LUMO orbital of  $C_2 (X^1 \Sigma_g^+)$ . The sum of the attractive  $(\Delta E_{\rm orb})$  and repulsive  $(\Delta E_{\rm Pauli})$  interactions of the electrons in the  $\sigma$  orbitals of dinitrogen contribute very little if anything to the N-N bond. Note also that the sum of  $\Delta E_{\rm orb}$  $(-730.0 \text{ kcal mol}^{-1})$  and  $\Delta E_{\text{Pauli}}$  (802.4 kcalmol<sup>-1</sup>) results in a repulsive contribution to  $\Delta E_{\text{int}}$ . According to the EPA, N<sub>2</sub> is a stable molecule only because of the strong contribution of the quasiclassical electrostatic interaction.

The results of the EPA of  $N_2$  have shown that the electrostatic attractions between the spherical nitrogen atoms, which amount to 30.0% of the total attraction, make a significant contribution to the nonpolar bond between two elements of the first octal row. The data also show that the Pauli repulsion plays a very important role in the strength of the chemical bond. In the next section we investigate the

differences in the nonpolar single bonds between atoms of the first octal row of the periodic system.

 $H<sub>n</sub>E-EH<sub>n</sub>$  bonds (E=Li to F;  $n=0-3$ ): Table 2 gives the most important results from the EPA of the  $H<sub>n</sub>E-EH<sub>n</sub>$ bonds  $(E=Li$  to F) and the calculated bond lengths. The complete geometries are given in the Supporting Information. The theoretical geometries and bond dissociation energies are in good agreement with experimental data, except for the bond energy of  $F_2$ . The theoretical BDE for  $F_2$  ( $D_0=$  $51.5$  kcalmol<sup>-1</sup>) is clearly higher than the experimental value  $(D_0=37.9 \text{ kcal mol}^{-1}).$ 

The calculations indicate that the C $-C$  bond of ethane has the largest interaction energy ( $\Delta E_{\text{int}} = -114.8 \text{ kcal mol}^{-1}$ ) of the E-E single bonds that were investigated in our study. The bond dissociation energy for ethane  $(D_e=93.1 \text{ kcal})$ mol<sup>-1</sup>) is significantly lower than the  $\Delta E_{\text{int}}$  value because of the rather large preparation energy  $(\Delta E_{\text{prep}}=21.7 \text{ kcal})$  $mol^{-1}$ ); CH<sub>3</sub> has a planar equilibrium structure, while the methyl groups in ethane have a pyramidal geometry. The ZPE-corrected bond dissociation energy  $(D_0=83.4 \text{ kcal})$  $mol^{-1}$ ) is in reasonable agreement with the experimental value of 89.9 kcal mol<sup>-1</sup>.

The breakdown of  $\Delta E_{\text{int}}$  into the three energy terms provides the most important result. Table 2 shows that the electrostatic attraction,  $\Delta E_{\text{elstat}}$ , is  $-130.9 \text{ kcal mol}^{-1}$ , which is 41.4% of the total attractive energy, while the orbital term,  $\Delta E_{\rm orb}$ , contributes -185.5 kcalmol<sup>-1</sup> (58.6%). The EPA reveals that, like the nitrogen-nitrogen bond in  $N_2$ , the quasiclassical electrostatic attraction between the methyl groups in ethane is stronger than the total interaction energy. It should be emphasized that this result does not depend on the partitioning procedure that was used in the bonding analysis. The only arbitrary decision made was the choice of methyl fragments for the analysis of the  $C-C$  bond in ethane.

Table 2 shows that the electrostatic character of the  $E-E$ bond increases monotonically from  $F-F(20.7%)$  to  $HBe-$  BeH  $(58.4\%)$  but then decreases for Li-Li  $(37.3\%)$ . The absolute values of  $\Delta E_{\text{elstat}}$  exhibit a less regular trend. There are several factors that determine the strength of the electrostatic attraction; the interatomic distance  $E-E$ , the nuclear charge of E and the topography of the electronic charge distribution. The latter can be visualized by analysis of the electron-density distribution. Figure 2a shows a contour line diagram of the Laplacian distribution of the electron density,  $\bigtriangledown^2 \rho(r)$ , of the CH<sub>3</sub> fragment in the frozen geometry of ethane. The Laplacian distribution has been found to be a sensitive probe for the topology of the electron-density distribution,  $\rho(r)$ .<sup>[40]</sup> The solid lines in Figure 2a show areas of relative electronic charge concentration, while the dashed



Figure 2. Contour line diagrams of the Laplacian distribution,  $\overline{\vee}^2 \rho(\mathbf{r})$ , of a) CH<sub>3</sub> calculated with the frozen geometry of  $H_3C$ –CH<sub>3</sub> and b) BeH calculated with the frozen geometry of HBe-BeH. Solid lines give areas of charge concentration  $[\nabla^2 \rho(r) < 0]$ , while dashed lines give areas of charge depletion  $[\nabla^2 \rho(r) > 0]$ .

Table 2. Energy decomposition analysis<sup>[a]</sup> of the H<sub>n</sub>E-EH<sub>n</sub> single bond (E=Li to F) at the BP86/TZ2P level of theory. Calculated atomic partial charges  $q_{\text{E}}$  and the E-E bond lengths are also given.

	Li <sub>2</sub>	Be <sub>2</sub> H <sub>2</sub>	$B_2H_4$	$C_2H_6$	$N_2H_4$	$O_2H_2$	F <sub>2</sub>
Symm.	$D_{\scriptscriptstyle{\infty}h}$	$D_{\scriptscriptstyle \infty h}$	$D_{2d}$	$D_{3d}$	$\mathcal{C}_{2}$	$C_{2}$	$D_{\scriptscriptstyle{\infty}h}$
$\Delta E_{\mathrm{int}}$	$-20.6$	$-70.3$	$-114.5$	$-114.8$	$-76.8$	$-62.6$	$-52.8$
$\Delta E_{\rm Pauli}$	1.9	41.1	161.7	201.6	407.9	384.6	145.8
$\Delta E_{\text{elstat}}^{[\text{b}]}$	$-8.4(37.3\%)$	$-65.1(58.4\%)$	$-140.5(50.9\%)$	$-130.9(41.4\%)$	$-178.3(36.8\%)$	$-145.8(32.6\%)$	$-41.1(20.7\%)$
$\Delta E_{\rm orb}^{\rm [b]}$	$-14.1(62.7\%)$	$-46.3(41.6\%)$	$-135.7(49.1\%)$	$-185.5(58.6\%)$	$-306.4(63.2\%)$	$-301.4(67.4\%)$	$-157.5(79.3\%)$
$\Delta E_{\sigma}^{[c]}$	$-14.1(100\%)$	$-46.3(100\%)$	$-119.7(88.2\%)$	$-175.5(94.6\%)$			$-151.3(96.1\%)$
$\Delta E_\pi^{[c]}$			$-16.0(11.8\%)$	$-10.0(5.4\%)$			$-6.2(3.9\%)$
$\Delta E_{\mathrm{prep}}$	$\Omega$	1.6	6.1	21.7	4.2	3.2	0
$D_e$	20.6	68.7	108.4	93.1	72.6	59.4	52.8
$D_0^{\text{[d]}}$	$20.1(26.4\pm1.0)$	64.9 $(71.7)^{[e]}$	103.0 $(104.0)^{[e]}$	83.4 $(89.9 \pm 0.5)$	62.8(65.8)	53.6 $(50.9 \pm 1.0)$	51.5 (37.9)
$q_{\rm E}$ [e]	0.0	0.196	0.081	$-0.105$	$-0.214$	$-0.153$	0.0
$E-E[\AA]^{[d]}$	2.737(2.673)	2.101 $(2.101)^{[f]}$	$1.623(1.656)^{[g]}$	1.532(1.535)	1.443 (1.449)	1.473 $(1.464)^{[h]}$	1.421(1.412)

[a] Energy values are given in kcalmol<sup>-1</sup>. [b] The percentage values in parentheses give the contribution to the total attractive interactions  $\Delta E_{\text{elsta}} + \Delta E_{\text{orb}}$ [c] The percentage values in parentheses give the contribution to the orbital interactions  $\Delta E_{\rm orb}$ . [d] The experimental values are given in parentheses. Unless otherwise noted they have been taken from ref. [35]. [e] The theoretical value was taken from high-level (CBS-Q) ab initio calculations, see ref. [36]. [f] The theoretical value was taken from ref. [37]. [g] The theoretical value was taken from ref. [38]. [h] Ref. [39].

lines indicate areas of relative charge depletion. We would like to point out that the Laplacian distribution does not show absolute charge concentrations. It indicates rather the differences in the charge concentration around the atoms with respect to monotonous decay. In a separated atom, the Laplacian distribution gives the shell structure of the electron density. For a bonded atom in a molecule, the Laplacian distribution gives the deformation of the spherical charge distribution which is caused by the interatomic interactions. The shape of the Laplacian distribution of a molecule shows the areas of charge concentration and charge depletion relative to the charge distribution of the free atoms.

The shape of the Laplacian distribution in Figure 2a clearly shows that the carbon atom of the methyl group has an area of charge concentration that is aligned in the direction of the carbon-carbon bond of ethane. This charge concentration can be interpreted as the electron density of an electron in an sp<sup>3</sup>-hybridized orbital. The important point is that the carbon atom of the methyl radical in ethane has a highly anisotropic valence-electron distribution that enhances the electrostatic attraction with the nucleus of the other carbon atom. The EPA of the nitrogen-nitrogen bond in  $N_2$  has shown, however, that fragments that have a spherically symmetrical charge distribution may strongly attract each other through classical electrostatic interactions. Hence, the anisotropy of the charge distribution enhances or weakens the  $\Delta E_{\text{elstat}}$  term.

The electron-density distribution in the BeH fragment of HBe-BeH shows an even larger area of charge concentration at the beryllium atom directed towards the other Be (Figure 2b). This is because beryllium is less electronegative than carbon and thus the charge distribution is more diffuse. The charge distribution around the lithium atom is isotropic, however, because the valence electron occupies the 2s AO (Figure 3a). The results of the calculations suggest that the topography of the electron-density distribution of the interacting fragments is very important for the relative strength of the  $\Delta E_{\text{elstat}}$  term. Note that according to the atomic partial charge,  $q_E$ , there should be electrostatic repulsion between the atoms in  $E-E$ . The repulsion should be particularly large for the N-N interactions in  $N_2H_4$ , which actually has the biggest absolute value of the electrostatic attractions in the  $H<sub>n</sub>E-EH<sub>n</sub>$  molecules (Table 2). This is because only the total atomic net charge is considered in the partial charges, which can be misleading because the topography of the valence-electron distribution is neglected.

The EPA calculations underestimate the contribution of the electrostatic attraction. This can be demonstrated by further analysis of the electronic structure of  $Li<sub>2</sub>$ . Figure 3a exhibits the Laplacian distribution,  $\bigtriangledown^2 \rho(r)$ , of lithium, which shows that an isotropic charge distribution,  $\rho(r)$ , is used to calculate  $\Delta E_{\text{elstat}}$ . Figure 3b shows the Laplacian distribution of lithium in  $Li<sub>2</sub>$ , which was calculated by using the frozen orbital coefficients of lithium in the diatomic molecule. It is evident that the valence-electron concentration of lithium is highly polarized towards the other lithium atom as the charge concentration is aligned along the Li-Li bond. The



Figure 3. Contour line diagrams of the Laplacian distribution,  $\bigtriangledown^2 \rho(\mathbf{r})$ , of a) the lithium atom calculated with complete SCF convergence and b) the lithium atom calculated with the frozen AO coefficients of Li<sub>2</sub>. The solid lines give areas of charge concentration  $[\nabla^2 \rho(r) < 0]$ , while the dashed lines give areas of charge depletion  $[\nabla^2 \rho(r) > 0]$ .

distorted electronic charge distribution of lithium will enhance the electrostatic attraction compared with the undistorted charge distribution because more negative charge is accumulated near the nucleus of the other lithium atom. It could be argued that  $\Delta E_{\text{elstat}}$  should be calculated by using the electron-density distribution shown in Figure 3b. However, this would be meaningless because the distorted charge distribution,  $\rho(r)$ , is a result of all the interatomic interactions including the orbital interactions.

So far in the discussion of the nature of the chemical bond in  $H<sub>n</sub>E-EH<sub>n</sub>$  we have focussed on the attractive energy contributions,  $\Delta E_{orb}$  and  $\Delta E_{elstat}$ , but the repulsive contribution of  $\Delta E_{\text{Pauli}}$  is also very important for understanding the strength of the bonding interactions. For example, the calculated  $\Delta E_{\text{Pauli}}$  value for H<sub>2</sub>N-NH<sub>2</sub> is very large (407.9 kcalmol<sup>-1</sup>), which is why the  $\Delta E_{\text{int}}$  value and the bond dissociation energy,  $D_e$ , are significantly lower than those of  $H_2B-BH_2$  and  $H_3C-CH_3$ . The strong Pauli repulsion arises from the interaction between the lone-pair electrons of the nitrogen atoms in the lowest-lying gauche conformation of hydrazine shown in Figure 4a. The attractive terms,  $\Delta E_{\text{elstat}}$  and  $\Delta E_{\text{orb}}$ , of H<sub>2</sub>N-NH<sub>2</sub> have the largest values of the  $H<sub>n</sub>E-EH<sub>n</sub>$  molecules, which indicates that the lower BDE of  $H_2N-NH_2$  relative to  $H_3C-CH_3$  is not caused by a weaker nitrogen–nitrogen attraction. The results of the EPA of  $H_2N-NH_2$  and  $H_2Be-BeH_2$  show that use of the net interaction energy,  $\Delta E_{\text{int}}$ , and the bond dissociation energy,  $D<sub>e</sub>$ , in a comparison of the nature of the chemical bonds may be misleading. These two molecules have very similar  $\Delta E_{\text{int}}$  and  $D_e$  values, but the Pauli repulsion in H<sub>2</sub>N-NH<sub>2</sub> is 10 times higher than in  $H_2Be-BeH_2$ . The Pauli repulsion in



Figure 4. Sketch of the calculated conformations of a)  $H_2N-NH_2$ , b)  $F_2N-NF_2$ , c) HO-OH and d) FO-OF. The theoretically predicted torsion angles are given in degree.

HO-OH, which comes from the interatomic interactions of the oxygen lone-pair electrons (see Figure 4c), is also very large  $(\Delta E_{Pauli}=384.6 \text{ kcalmol}^{-1})$  and hence the reason for the rather low BDE.

The calculated energy terms of the fluorine-fluorine bond in  $F<sub>2</sub>$  are good examples with which to demonstrate the insight that has been gained through the EPA. It is well known that  $F_2$  has a lower BDE than Cl<sub>2</sub>. This is usually explained by the interatomic Pauli repulsion of the fluorine lone-pair electrons, which is expected to be rather strong owing to the short F-F interatomic distance. However, recent investigations of the chemical bonds in the dihalogen molecules  $X_2$  (X=F to I) using the EPA method have shown that the small BDE of  $F_2$  is in fact due to the unusually weak quasiclassical electrostatic attraction between the fluorine atoms.<sup>[41]</sup> Fluorine is the most electronegative element and has a small atomic radius because of the compact electron-density distribution. Hence the electron density of the fluorine atom only overlaps with the nucleus of the other fluorine atom to a small extent.

It seems possible that the much weaker bond of  $F_2$  $(\Delta E_{\text{int}} = -52.8 \text{ kcal mol}^{-1})$  relative to that of  $H_2B-BH_2$  $(\Delta E_{\text{int}} = -114.5 \text{ kcal mol}^{-1})$  can also be explained by the difference between the  $\Delta E_{\text{elstat}}$  values. Alternatively F<sub>2</sub> may

 $=$  -41.1 kcalmol<sup>-1</sup>). The low  $\Delta E_{\text{elstat}}$  value can be attributed to the compact 2p orbital of the most electronegative element, fluorine, which prevents a strong attraction between the unpaired electron in the  $2p(\sigma)$  AO of one fluorine atom and the nucleus of the other. The same argument explains why the Pauli repulsion in  $F_2$  is much weaker than that in  $HO$ -OH and  $H_2N$ -NH<sub>2</sub>.

Table 2 also includes the  $\sigma$  and  $\pi$  contributions to the E-E orbital interactions in molecules that possess a mirror plane. The  $\pi$ -bonding contributions to  $\Delta E_{\rm orb}$  in B<sub>2</sub>H<sub>4</sub>, C<sub>2</sub>H<sub>6</sub> and  $F_2$  are, as expected, rather small. The strength of the hyperconjugative interactions in  $H_2B-BH_2$  ( $D_{2d}$ ) is 16.0 kcal mol<sup>-1</sup>, which is 11.8% of the total  $\Delta E_{\text{int}}$  term. This means that the empty  $p(\pi)$  orbital of boron is stabilized by one B-H bond by  $4.0 \text{ kcalmol}^{-1}$ . A detailed EPA of the boronboron bond in  $X_2B-BX_2$  (X=H, F, Cl, Br, and I) has been presented somewhere else.[22l]

 $\mathbf{F}_n \mathbf{E} - \mathbf{E} \mathbf{F}_n$  bonds ( $\mathbf{E} = \mathbf{B}$ e to O;  $n = 1-3$ ): We analyzed the E-E bonding in molecules of FBe-BeF,  $F_2B-BF_2$ ,  $F_3C-CF_3$ ,  $F_2N-NF_2$ , and FO-OF by the EPA method in order to learn about the effect of fluorine substitution on the nature of the bond. The results are given in Table 3.

The results of the EPA show that the ratio of the contribution of electrostatic and orbital interactions to the  $E$ -E bond does not change much when hydrogen is substituted by fluorine. The relative contributions of the electrostatic attraction to the binding interactions in  $F<sub>n</sub>E-EF<sub>n</sub>$  are as high as in H<sub>n</sub>E-EH<sub>n</sub>. In the former compounds the  $\Delta E_{\text{elstat}}$  term constitutes between 29.8 ( $E = O$ ) and 55.3% ( $E = Be$ ) of the attractive interactions. Previous theoretical studies have indicated that several of the properties of these molecules change very little when hydrogen atoms are replaced by fluorine atoms.[47] However, there are surprising differences in the bond strengths of  $F_nE-EF_n$  and  $H_nE-EH_n$ , which will be analyzed with the help of the EPA data.

Comparison of the calculated interaction energy values  $\Delta E_{\text{int}}$  of the F<sub>n</sub>E-EF<sub>n</sub> bond (Table 3) with the  $\Delta E_{\text{int}}$  values of

have a weaker bond than  $H_2B-BH_2$  because the former has a larger Pauli repulsion due to its lone-pair electrons which the latter does not have. The data in Table 2 does not support this reasoning. Comparison of the results for  $F_2$ and  $H_2B$ -BH<sub>2</sub> shows that the orbital interactions in difluorine  $(\Delta E_{\rm orb} = -157.5 \text{ kcal mol}^{-1})$ are stronger than those in  $H_2B-BH_2$  and that the Pauli repulsion  $(\Delta E_{\text{Pauli}}=145.8 \text{ kcal})$  $mol^{-1}$ ) is weaker. The weaker bond of  $F_2$  compared with  $H_2B$ -BH<sub>2</sub> is therefore a result of the significantly weaker electrostatic attraction ( $\Delta E_{\text{elstat}}$ 

Table 3. Energy decomposition analysis<sup>[a]</sup> of the  $F<sub>n</sub>E-EF<sub>n</sub>$  single bond (E=Be to O) at the BP86/TZ2P level of theory. Calculated atomic partial charges  $q_E$  and the E-E bond lengths are also given.

	$Be_2F_2$	$B_2F_4$	$C_2F_6$	$N_2F_4$	$O_2F_2$	
Symm.	$D_{\scriptscriptstyle{\infty h}}$	$D_{2d}$	$D_{3d}$	$C_{2}$	$C_{2}$	
$\Delta E_{\text{int}}$	$-71.8$	$-102.6$	$-92.9$	$-21.7$	$-97.6$	
$\Delta E_{\rm Pauli}$	26.3	123.8	253.9	323.1	614.4	
$\Delta E_{\text{elstat}}^{[\text{b}]}$	$-54.2(55.3\%)$	$-116.5(51.5\%)$	$-150.2(43.4\%)$	$-130.6(37.9\%)$	$-212.0(29.8\%)$	
$\Delta E_{\rm orb}^{\rm [b]}$	$-43.9(44.7\%)$	$-109.9(48.5\%)$	$-196.6(56.6%)$	$-214.2(62.1\%)$	$-500.0(70.2\%)$	
$\Delta E_{\alpha}^{[c]}$	$-43.8(99.8\%)$	$-105.3(95.8\%)$	$-184.2(93.7%)$			
$\Delta E_{\pi}^{[c]}$	$-0.1(0.2\%)$	$-4.6(4.2\%)$	$-12.4(6.3\%)$			
$\Delta E_{\mathrm{prep}}$	1.3	4.1	5.6	4.6	36.0	
$D_{\scriptscriptstyle e}$	70.5	98.5	87.3	17.1	61.6	
$D_0^{[d]}$	68.4	95.2	84.3 $(96.9 \pm 2)^{[e]}$	14.2 $(21 \pm 1)^{[e]}$	59.2 $(48)$ <sup>[f]</sup>	
$q_{\rm E}$ [e]	0.268	0.247	0.221	0.113	0.159	
$E-E[\AA]^{[d]}$	2.050	$1.725$ $(1.719)^{[g]}$	$1.567 (1.545)^{[h]}$	$1.527 (1.492)^{[i]}$	$1.204$ $(1.217)^{[j]}$	

[a] Energy values in kcalmol<sup>-1</sup>. [b] The percentage values in parentheses give the contribution to the total attractive interactions  $\Delta E_{\text{elstat}} + \Delta E_{\text{orb}}$ . [c] The percentage values in parentheses give the contribution to the orbital interactions  $\Delta E_{\rm orb}$ . [d] The experimental values are given in parentheses. [e] Ref. [42]. [f] On the basis of the heats of formation of FOOF and OF, which are reported in ref. [43]. [g] Ref. [44]. [h] Ref. [35]. [i] Ref. [45]. [j] Ref. [46].

the respective hydrogen-substituted analogues  $H<sub>n</sub>E-EH<sub>n</sub>$ (Table 2) shows that the fluorine atom has a non-uniform effect on the interaction energies. FBe-BeF and HBe-BeH have nearly the same  $\Delta E_{\text{int}}$  values, whereas the fluorine analogues,  $F_2B-BF_2$  and  $F_3C-CF_3$ , have smaller interaction energies than the corresponding hydrogen systems. The interaction energy of N<sub>2</sub>F<sub>4</sub> ( $\Delta E_{\text{int}} = -21.7 \text{ kcal mol}^{-1}$ ) is much smaller than that of  $N_2H_4$  ( $\Delta E_{\text{int}} = -76.8 \text{ kcal mol}^{-1}$ ), while  $O_2F_2$  ( $\Delta E_{\text{int}} = -97.6 \text{ kcalmol}^{-1}$ ) has a significantly larger interaction energy than  $O_2H_2$  ( $\Delta E_{int} = -62.6 \text{ kcal mol}^{-1}$ ). The analysis of the energy terms should enable a better understanding of the peculiar trend of the calculated  $\Delta E_{\text{int}}$  values.

Inspection of the energy contributions to  $\Delta E_{\text{int}}$  of FBe-BeF (Table 3) shows that the absolute values of  $\Delta E_{\text{elstat}}$ ,  $\Delta E_{\text{panti}}$ , and  $\Delta E_{\text{orb}}$  are smaller than those of HBe-BeH (Table 2) even though the former compound has a shorter Be-Be bond than the latter. The FBe-BeF bonding orbital has a higher percentage s character and is therefore more compact than the HBe-BeH s orbital because fluorine is more electronegative than hydrogen.[48] The repulsive and attractive beryllium–beryllium interactions in FBe-BeF are therefore weaker than those in HBe-BeH but the sum of the energy contributions in the two molecules yields nearly the same  $\Delta E_{\text{int}}$  value. Note that the B-B distance in F<sub>2</sub>B- $BF_2$  is significantly longer (1.725 Å) than that in  $H_2B-BH_2$  $(1.623 \text{ Å})$ , which is in contrast to the findings with the beryllium system in which the substitution of hydrogen by fluorine causes a shortening of the central bond. This can be explained by consideration of the  $\pi$ -bonding contribution to the  $D_{2d}$  equilibrium structures of  $F_2B-BF_2$  and  $H_2B-BH_2$ . The B-H bonding orbital is a better hyperconjugative donor than the  $B-F$  bonding orbital. The latter orbitals contribute only 4.6 kcalmol<sup>-1</sup> to the B-B bond (Table 3) while the  $\pi$ bonding contribution to the B-H bonds is  $16.0 \text{ kcalmol}^{-1}$ (Table 2). The  $F_2B-BF_2$  bond becomes shorter than the  $H_2B-BH_2$  bond when the hyperconjugative interactions are turned off. Geometry optimization of planar  $(D_{2h})$  structures gives bond lengths of 1.734 (F<sub>2</sub>B-BF<sub>2</sub>) and 1.752 Å (H<sub>2</sub>B-BH<sub>2</sub>). Hence, the HBe-BeH and FBe-BeF bonding interactions are mainly determined by direct Be-Be contact while the F<sub>2</sub>B-BF<sub>2</sub> and H<sub>2</sub>B-BH<sub>2</sub> bonding interactions in the  $D_{2d}$ equilibrium structures are significantly influenced by the hydrogen and fluorine substituents.

The interaction energy of  $F_3C-CF_3$  ( $\Delta E_{\text{int}} = -92.9$  kcal mol<sup>-1</sup>) is clearly smaller than that of  $H_3C$ -CH<sub>3</sub> ( $\Delta E_{\text{int}}$ =  $-114.8$  kcalmol<sup>-1</sup>) even though the electrostatic attraction and orbital interactions in the former compound are stronger than in the latter. The smaller  $\Delta E_{\text{int}}$  value for the former molecule can be explained in terms of the much higher Pauli repulsion in  $F_3C-CF_3$ , which is caused by the fluorine's lone-pair electrons. Note that the bond dissociation energy of  $F_3C$ -C $F_3$  (calculated  $D_0 = 84.3$  kcalmol<sup>-1</sup>; experimental  $D_0$ =96.9 kcalmol<sup>-1</sup>) is greater than that of  $H_3C$ –CH<sub>3</sub> (calculated  $D_0 = 83.4 \text{ kcal mol}^{-1}$ ; experimental  $D_0 = 89.9 \text{ kcal}$  $mol^{-1}$ ). Two factors are responsible for this. One factor is significantly smaller preparation energy of the  $CF_3$  groups  $(\Delta E_{\text{prep}} = 5.6 \text{ kcalmol}^{-1})$  compared with that of the CH<sub>3</sub>

groups  $(\Delta E_{\text{prep}} = 21.7 \text{ kcal mol}^{-1})$ . The second factor that leads to the higher bond dissociation energy of  $F_3C-CF_3$  is the smaller contribution of the zero-point vibrational energy  $(3.0 \text{ kcal mol}^{-1})$  compared with that for  $H_3C$ –C $H_3$  (9.7 kcal mol<sup>-1</sup>). The contributions of the  $\pi$  bonding to the  $\Delta E_{\rm orb}$  of  $F_3C-CF_3$  (-12.4 kcalmol<sup>-1</sup>) and  $H_3C-CH_3$  (-10.0 kcal  $mol<sup>-1</sup>$ ) are similar although this property only plays a minor role in the C-C bond of these molecules.

The energy-partitioning analysis of  $F_2N-NF_2$  was carried out by using the gauche conformation of the molecule (Figure 4b) in order to compare the results with those for the hydrazine molecule, which has a gauche equilibrium geometry. A recent experimental study of the conformational stability of  $N_2F_4$  by Raman spectroscopy showed that the gauche and trans conformations are energetically nearly degenerate.[49] The enthalpy difference was determined to be  $0.197 \pm 0.017$  kcalmol<sup>-1</sup> with the *trans* conformer the most stable rotamer.

 $F_2N-NF_2$  has the smallest  $\Delta E_{\text{int}}$  value  $(-21.7 \text{ kcal mol}^{-1})$ of the  $F<sub>n</sub>E-EF<sub>n</sub>$  compounds (Table 3). Comparison of the energy components of the N-N bond in  $F_2N-NF_2$  with those in  $H_2N-NH_2$  (Table 2) shows that the absolute values of  $\Delta E_{\text{Pauli}}$ ,  $\Delta E_{\text{elstat}}$ , and  $\Delta E_{\text{orb}}$  in the former compound are smaller than those in the latter. This appears reasonable because  $F_2N-NF_2$  has a significantly longer N-N bond  $(1.527 \text{ Å})$  than H<sub>2</sub>N–NH<sub>2</sub> (1.443 Å). Shortening of the F<sub>2</sub>N–  $NF<sub>2</sub>$  distance would result in a steep increase in the Pauli repulsion because the lone pairs on the fluorine atoms of the adjacent  $NF<sub>2</sub>$  groups would be closer to each other. Note, however, that  $F_3C-CF_3$  also has a longer central bond than  $H_3C$ – $CH_3$  and yet the former compound has larger values of  $\Delta E_{\text{Pauli}}$ ,  $\Delta E_{\text{elstat}}$ , and  $\Delta E_{\text{orb}}$  than the latter. The differences between the carbon and nitrogen systems can be explained by the shorter E-E bond length of  $H_2N-NH_2$  (1.443 Å) relative to that of  $H_3C$ –CH<sub>3</sub> (1.532 Å) and by the lone pairs in the former compound, which also yield a strong Pauli repulsion in the hydrogen-substituted compound.

The most surprising result of the energy analysis of the  $F<sub>n</sub>E-EF<sub>n</sub>$  compounds is the very strong interaction energy of FO-OF ( $\Delta E_{\text{int}} = -97.6 \text{ kcal mol}^{-1}$ ). The calculated bond dissociation energy ( $D_e$ =61.6 kcalmol<sup>-1</sup>) is much smaller than the  $\Delta E_{\text{int}}$  value because the preparation energy of the OF fragments is rather high. The O $-F$  distance in FO $-OF$  is clearly longer (1.608 Å) than that in free OF (1.366 Å). The lengthening of the  $O-F$  distance on formation of  $FO-OF$  is in agreement with the experimental $[46]$  and previous theoretical<sup>[50]</sup> results. Inspection of the energy terms (Table 3) shows that the contribution of the orbital interactions to the oxygen-oxygen bond is very large  $(\Delta E_{orb} = -500.0 \text{ kcal})$ mol<sup>-1</sup>). The large value of the  $\Delta E_{orb}$  term relative to that for HO-OH compensates for the greater Pauli repulsion  $(614.4 \text{ kcal mol}^{-1})$  in FO-OF. The O-O bond length in FO-OF is much shorter  $(1.204 \text{ Å})$  than that in HO-OH  $(1.473 \text{ Å})$ . It is striking that substitution of the hydrogen atoms in  $H_3C$ -CH<sub>3</sub> and  $H_2N-NH_2$  by fluorine leads to longer interatomic distances and smaller interaction energies for the central C-C and N-N bonds, while the central bond

length in FO-OF is much shorter and the  $\Delta E_{\text{int}}$  value is significantly higher than for HO-OH. This can be explained in terms of the Pauli repulsion between the fluorine's lone-pair electrons in FO $-OF$ , which can be reduced by rotation about the  $O-O$  bond (Figure 4d). This is not possible in  $F_3C-CF_3$  and  $F_2N-NF_2$  because any rotation about the C-C or N-N bond that reduces the Pauli repulsion between one pair of adjacent fluorine atoms will enhance the Pauli repulsion between other fluorine atoms (see Figure 4b for  $F_2N$ - $NF<sub>2</sub>$ ). Note that the calculated FO-OF dihedral angle is 89.4 $\degree$  (experimental value 87.5 $\degree$ ),<sup>[46]</sup> which shows that the molecule tries to minimize the F–F repulsion in the gauche conformation. The Pauli repulsion between the fluorine atoms would be even weaker in the trans conformer, but then the favorable hyperconjugation between the oxygen's lone-pair electrons and the *trans*  $O-F \sigma^*$  orbitals would be lost.

Multiple bonds in HB=BH,  $\rm H_2C{=}\rm CH_2, \ HC{\equiv}\rm CH, \ and \ HN=$ NH: We analyzed the double bonds between elements of the first octal row in the homopolar molecules HB=BH,  $H_2C=CH_2$ , and the *trans* form of HN=NH. The calculations on the boron species  $B_2H_2$  were performed on the  $({}^1\Sigma_g^{\ +})$ singlet state ( $D_{\omega h}$  symmetry), which is an excited state, because we wanted to compare the strength of the boron boron  $\pi$  bond with the other molecules: B<sub>2</sub>H<sub>2</sub> has a  $({}^{3}\Sigma_{g}^{-})$ triplet ground state.[51] We also investigated the triple bond in acetylene, HC=CH. The EPA results are given in Table 4.

The contributions of the electrostatic attraction to the binding interactions of the multiple bonds are smaller than

Table 4. Energy decomposition analysis<sup>[a]</sup> of the HB=BH, H<sub>2</sub>C=CH<sub>2</sub>, trans-HN=NH and HC=CH multiple bonds at the BP86/TZ2P level of theory. Calculated atomic partial charges  $q_E$  and the E-E bond lengths are also given.

$\check{ }$				
	$B_2H_2$	$C_2H_4$	$trans-N, H,$	$C_2H_2$
Symm.	$D_{\scriptscriptstyle{\infty}h}$	$D_{2h}$	$C_{2h}$	$D_{\infty h}$
$\Delta E_{\mathrm{int}}$	$-159.8$	$-191.1$	$-137.4$	$-280.0$
$\Delta E_{\rm Pauli}$	116.3	281.9	599.4	255.4
$\Delta E_{\mathrm{elstat}}^{[\mathrm{b}]}$	$-110.6$	$-181.6$	$-254.6$	$-147.5$
	$(40.1\%)$	$(38.4\%)$	$(34.6\%)$	$(27.6\%)$
$\Delta E_{\rm orb}{}^{\textrm{[b]}}$	$-165.5$	$-291.4$	$-482.2$	$-387.9$
	$(59.9\%)$	$(61.6\%)$	$(65.4\%)$	$(72.4\%)$
$\Delta E_\sigma^{[c]}$	$-111.1$	$-212.2$	$-392.6$	$-215.5$
	$(67.1\%)$	$(72.8\%)$	$(81.4\%)$	$(55.6\%)$
$\Delta E_{\pi}^{[c]}$	$-54.4$	$-79.2$	$-89.6$	$-172.4$
	$(32.9\%)$	$(27.2\%)$	$(18.6\%)$	$(44.4\%)$
$\Delta E_{\rm{prep}}$	4.4	12.9	5.6	32.8
$D_e$	155.4	178.2	131.8	247.2
$D_0^{\text{[d]}}$	149.8	168.3	123.7	238.7
		$(175.4 \pm 2)$	$(123.8 \pm 1)^{[e]}$	$(230.9 \pm 2)$
$q_{\rm E}$ [e]	0.031	$-0.086$	$-0.106$	$-0.093$
$E-E$	1.526	1.333	1.249	1.206
$[A]^{[d]}$	$(1.498)$ <sup>[f]</sup>	(1.339)	$(1.252)^{[g]}$	(1.203)

[a] Energy values are given in kcalmol<sup>-1</sup>. [b] The percentage values in parentheses give the contribution to the total attractive interactions  $\Delta E_{\text{elstat}} + \Delta E_{\text{orb}}$ . [c] The percentage values in parentheses give the contribution to the orbital interactions  $\Delta E_{\text{orb}}$ . [d] The experimental values are given in parentheses. Unless otherwise noted they have been taken from ref. [35]. [e] Ref. [52]. [f] The theoretical values was taken from ref. [53]. [g] Ref. [54].

in the respective single bonds (Table 2) but they are still rather large. The  $H<sub>n</sub>E=EH<sub>n</sub>$  double bonds possess between 34.6  $(E=N)$  and 40.1%  $(E=B)$  electrostatic character. Thus, more than one third of the total interatomic attraction comes from electrostatic forces. The contribution of  $\Delta E_{\text{elstat}}$ to the binding interactions of  $HC=CH$  is still 27.6%.

The calculated HB=BH bond length is clearly shorter  $(1.526 \text{ Å})$  than that of H<sub>2</sub>B-BH<sub>2</sub> (1.623 Å) and the estimated interaction energy of the former compound  $(\Delta E_{\text{int}}$  $-159.8$  kcalmol<sup>-1</sup>) is significantly larger than that of the latter ( $\Delta E_{\text{int}} = -114.5 \text{ kcalmol}^{-1}$ ). How much of the increase in  $\Delta E_{\text{int}}$  can be attributed to the boron-boron  $\pi$  bond? The results in Table 4 show that the contribution of  $\Delta E_{\rm orb}$  to the HB=BH bond is larger (absolute value:  $-165.5$  kcalmol<sup>-1</sup>; relative value 59.9%) than the contribution of  $\Delta E_{orb}$  to the H<sub>2</sub>B-BH<sub>2</sub> bond. However, the  $\sigma$  contribution to  $\Delta E_{orb}$  of HB=BH is actually less  $(\Delta E_{\sigma} = -111.1 \text{ kcal mol}^{-1})$  than that to  $\Delta E_{\rm orb}$  of H<sub>2</sub>B-BH<sub>2</sub> ( $\Delta E_{\rm o}$  = -119.7 kcalmol<sup>-1</sup>). This means that the  $\pi$ -bonding interactions in HB=BH lead to a reduction in the  $\sigma$ -bond strength, which is compensated by the enhanced  $\pi$ -bond strength. Table 4 shows that  $\Delta E_{\pi}$  contributes  $-54.4$  kcalmol<sup>-1</sup> (32.9%) to  $\Delta E_{orb}$  while  $\Delta E_{g}$  contributes  $-111.1$  kcalmol<sup>-1</sup> (67.1%). It follows that the  $\pi$  bond in  $HB=BH$  is half as strong as the  $\sigma$  bond. The electrostatic attraction and the Pauli repulsion in HB=BH are clearly weaker than in  $H_2B-BH_2$ .

The interaction energy in ethylene is also higher ( $\Delta E_{\text{int}}$ =  $-191.1$  kcalmol<sup>-1</sup>) than in ethane  $(\Delta E_{\text{int}} = -114.8$  kcal  $mol<sup>-1</sup>$ ), but in contrast to the boron systems all the energy components of the doubly bonded molecule are larger than those of the singly bonded species. The contribution of the orbital interactions to the carbon=carbon double bond in ethylene is slightly larger (61.6%) than to the carbon carbon single bond in ethane (58.6%). The  $\pi$ -bond strength in H<sub>2</sub>C=CH<sub>2</sub> ( $\Delta E_{\pi}$ = -79.2 kcalmol<sup>-1</sup>) amounts to 27.2% of the total orbital interactions, while the  $\sigma$  contribution  $(\Delta E_{\sigma} = -212.2 \text{ kcal mol}^{-1})$  is 72.8% of  $\Delta E_{\text{orb}}$ . This means that the  $\pi$ -bond strength in ethylene has approximately one third the strength of the  $\sigma$  bond.

We wish to point out that the EPA of  $\Delta E_{\text{int}}$  gives a much more direct estimate of the  $\pi$ -bond strength than the calculation or the measurement of the rotational barrier of the molecule since rotation about a double bond also affects the other energy components of the chemical bond, that is, the  $\sigma$  bonding, electrostatic attraction, and nuclear repulsion.

The data in Table 4 show that the  $N=N$  interaction energy of *trans*-diazene is also much higher  $(\Delta E_{\text{int}} = -137.4 \text{ kcal})$  $mol^{-1}$ ) than the N-N interaction energy of hydrazine  $(\Delta E_{\text{int}} = -76.8 \text{ kcal mol}^{-1})$ , but is clearly less than the  $\Delta E_{\text{int}}$ value of ethylene. The absolute values of the energy components of HN=NH are significantly higher than those of ethylene, but the very strong Pauli repulsion in diazene  $(\Delta E_{\text{Pauli}} = 599.4 \text{ kcal mol}^{-1})$  leads to a weaker net attraction. Note that the absolute values of the  $\pi$ -bonding interactions increase from  $HB=BH$  to  $H_2C=CH_2$  and  $HN=NH$ , while the percentage  $\Delta E_{\pi}$  decreases (Table 4).

The EPA results suggest (Table 4) that the much higher interaction energy of acetylene  $(\Delta E_{\text{int}} = -280.0 \text{ kcal mol}^{-1})$ compared with that of ethylene  $(\Delta E_{\text{int}} = -191.1 \text{ kcal mol}^{-1})$ comes from the increase in the strength of the orbital interactions. The electrostatic attraction in HC $\equiv$ CH ( $\Delta E_{\text{elstst}}$ =  $-147.5$  kcalmol<sup>-1</sup>) is weaker than that in  $H_2C=CH_2$  $(\Delta E_{\text{elstst}} = -181.6 \text{ kcal mol}^{-1}),$ whereas the  $\Delta E_{\rm orb}$  value of the  $C\equiv C$  triple bond  $(-387.9 \text{ kcal})$  $mol^{-1}$ ) is much higher than that of the double bond  $(-291.4 \text{ kcal mol}^{-1})$ . The increase in  $\Delta E_{\rm orb}$  is nearly exclusively a result of the  $\pi$ -bonding



	$C_2H_6$	Si <sub>2</sub> H <sub>6</sub>	$Ge_2H_6$	$Sn_2H_6$	$Pb_2H_6$
Symm.	$D_{3d}$	$D_{3d}$	$D_{3d}$	$D_{3d}$	$D_{3d}$
$\Delta E_{\text{int}}$	$-114.8$	$-75.2$	$-69.7$	$-58.8$	$-48.2$
$\Delta E_{\rm Pauli}$	201.6	101.2	114.4	98.3	84.0
$\Delta E_{\text{elstat}}^{[b]}$	$-130.9(41.4\%)$	$-83.8(47.5\%)$	$-95.2(51.7%)$	$-86.6(55.1\%)$	$-68.3(51.7\%)$
$\Delta E_{\rm orb}$ [b]	$-185.5(58.6\%)$	$-92.6(52.5\%)$	$-88.9(48.3\%)$	$-70.5(44.9\%)$	$-63.9(48.3\%)$
$\Delta E_{\alpha}^{[c]}$	$-175.5(94.6\%)$	$-87.8(94.8\%)$	$-84.3(94.8)$	$-67.5(95.7%)$	$-61.2(95.8)$
$\Delta E_\pi^{[c]}$	$-10.0(5.4\%)$	$-4.8(5.2\%)$	$-4.6$ (5.2%)	$-3.0(4.3\%)$	$-2.7(4.2)$
$\Delta E_{\mathrm{prep}}$	21.7	2.8	$2.2^{\circ}$	1.4	1.4
$D_e^{[d]}$	93.1	72.4	67.5	$57.4(61.3)^{[e]}$	46.8
$D_0^{[d]}$	83.4 $(89.9 \pm 0.5)^{[f]}$	68.3 $(74 \pm 3)^{[g]}$	63.8 $(70.2)^{[h]}$	54.4	43.6
$q_{\rm E}$ [e]	$-0.105$	0.208	0.184	0.263	0.250
$E-E[\AA]^{[d]}$	$1.532(1.535)^{[f]}$	$2.352(2.331)^{[f]}$	2.418 $(2.403)^{[f]}$	2.786 $(2.758)^{[e]}$	$2.898(2.897)^{[i]}$

[a] Energy values in kcalmol<sup>-1</sup>. [b] The percentage values in parentheses give the contribution to the total attractive interactions  $\Delta E_{\text{elstat}} + \Delta E_{\text{orb}}$ . [c] The percentage values in parentheses give the contribution to the orbital interactions  $\Delta E_{\rm orb}$ . [d] The experimental values are given in parentheses. [e] The theoretical value was taken from ref. [55]. [f] Ref. [35]. [g] Ref. [42]. [h] The theoretical value was taken from ref. [56]. [i] The theoretical value was taken from ref. [57].

interactions in acetylene. The data in Table 4 indicate that the strength of the  $\pi$  bonding in HC=CH ( $\Delta E_{\pi}$ =  $-172.4$  kcalmol<sup>-1</sup>) is much higher than in H<sub>2</sub>C=CH<sub>2</sub> ( $\Delta E_{\pi}$ =  $-79.2$  kcalmol<sup>-1</sup>), while the  $\sigma$ -bond strength in HC=CH  $(\Delta E_{\sigma} = -215.5 \text{ kcal mol}^{-1})$  is nearly the same as in H<sub>2</sub>C=CH<sub>2</sub>  $(\Delta E_{\sigma} = -212.2 \text{ kcal mol}^{-1})$ . This is not surprising because acetylene has a degenerate  $\pi$  orbital which has two components while the  $\pi$  orbital of ethylene has only one. The calculated data suggest that each of the  $\pi$ -orbital components of acetylene has about the same strength as the  $\pi$  orbital in ethylene. The  $\pi$ -bond strength in acetylene contributes 44.4% to the total orbital interactions.

Finally, we compare the  $C \equiv C$  triple bond in acetylene with the triple bond in dinitrogen (Table 1). The calculated energy terms show that the triple bond in  $C_2H_2$  has a significantly larger interaction energy than that in  $N_2$  as a result of the much weaker Pauli repulsion in the former bond. The attractive interactions in the N $\equiv$ N bond ( $\Delta E_{\text{elstst}} + \Delta E_{\text{orb}} =$  $-1042.9$  kcalmol<sup>-1</sup>) are nearly twice as high as those in the HC≡CH bond ( $\Delta E_{\text{elstst}} + \Delta E_{\text{orb}} = -535.4 \text{ kcal mol}^{-1}$ ), although the difference between the  $\Delta E_{\text{Pauli}}$  strengths is even greater.

 $H_3E-EH_3$  bonds ( $E=C$  to Pb): We have also investigated the changes in the nature of the  $H_3E$ -EH<sub>3</sub> homopolar bonds along the Group 14 elements:  $E=C$ , Si, Ge, Sn, and Pb. Table 5 gives the results of the EPA.

The calculated data predict that the interaction energies  $\Delta E_{\text{int}}$  decrease monotonically from the lightest member of the series  $H_3C$ –C $H_3$  ( $\Delta E_{\text{int}}$  = -114.8 kcalmol<sup>-1</sup>) to the heaviest H<sub>3</sub>Pb-PbH<sub>3</sub> ( $\Delta E_{\text{int}} = -48.2 \text{ kcalmol}^{-1}$ ). The dissociation energies,  $D_e$  and  $D_0$ , display the same trend. With the exception of ethane, the absolute values of the interaction energies are only slightly larger than the  $D<sub>e</sub>$  values because the preparation energies are rather small.

The electrostatic nature of the  $H_3E$ -EH<sub>3</sub> bond increases from  $E=C$  to  $E=Sn$ . The lead-lead bond has a slightly higher percentage contribution from the orbital interactions than the tin-tin bond, which might be caused by relativistic effects which are particularly strong in lead compounds.<sup>[58]</sup> Apart from this, the changes in the nature of the  $H_3E$ – $EH_3$ bond and the strengths of the energy terms along the series from carbon to lead are uniform. Note, however, that the absolute values of the Pauli repulsion and electrostatic attraction in  $H_3Ge-GeH_3$  are larger than in  $H_3Si-SiH_3$ , possibly due to the filled 3d shell and the resulting contracted atomic radius of Ge relative to Si.

#### Summary

The interaction energy of a chemical bond can be meaningfully interpreted in terms of quasiclassical electrostatic interaction, Pauli repulsion, and orbital interactions. The contributions of all three terms must be considered when chemical bonds are compared. Chemical bonding is caused by classical electrostatic interactions and by the specific quantum mechanical kinematics of electrons, which result in the Pauli repulsion of occupied overlapping orbitals and the resonance and deformation of partially occupied orbitals.

The results of the EPA show that nonpolar covalent bonds between main-group elements of the first and higher octal rows of the periodic table have large contributions from quasiclassical electrostatic attractions between the bonded fragments that may be even stronger than orbital interactions. The bonding interactions in  $H_nE-EH_n$  (E=Li to F;  $n=0-3$ ) possess between 20.7 (E=F) and 58.4% (E= Be) electrostatic character. The nature of the bonding interactions in  $H<sub>2</sub>$ , which comes exclusively from orbital interactions, is atypical of chemical bonds. The electrostatic bonding arises from the attraction between areas of electronic charge concentration in the valence-shell distribution of one atom and the nucleus of the other atom. With the exception of lithium, the electronic charge distribution in the valence shell of E in the fragment  $H<sub>n</sub>E$  is highly anisotropic. Howev-

### er, even fragments with a spherically symmetrical electronic charge distribution may strongly attract each other through quasiclassical electrostatic forces. This is evident from the calculated value  $\Delta E_{\text{elstat}} = -312.9 \text{ kcal mol}^{-1}$  for N<sub>2</sub>. A true understanding of the nature of the chemical bond can only be achieved when the Pauli repulsion is considered. The binding interactions in  $H_2N-NH_2$  and HO-OH are weakened by strong Pauli repulsion.

The substitution of hydrogen by fluorine does not lead to significant changes in the nature of the binding interactions in  $F<sub>n</sub>E-EF<sub>n</sub>$  (E=Be to O), that is, the relative strengths of the orbital interactions and electrostatic attraction change little although the absolute values may change substantially. The fluorine substituents have a large effect on the Pauli repulsion in the nitrogen and oxygen compounds, which explains why  $F_2N-NF_2$  has a much weaker bond than  $H_2N NH<sub>2</sub>$ , while the interaction energy in FO-OF is much stronger than in HO-OH.

The double bonds in HB=BH,  $H_2C=CH_2$ , and HN=NH have a higher degree of orbital interactions than the corresponding single bonds in  $H<sub>n</sub>E-EH<sub>n</sub>$ . Orbital interactions make an even bigger contribution to the covalent bonding in the HC=CH triple bond. The relative contribution of the  $\Delta E_{\text{elstat}}$  term increases whilst that of the  $\pi$  bonding decreases as E becomes more electronegative. The  $\pi$ -bonding interactions in HC=CH amount to 44.4% of the total orbital interactions. The interaction energy in  $H_3E$ –E $H_3$  (E=C to Pb) decreases monotonically as the element E becomes heavier. The electrostatic character of the E-E bond increases from  $E=C$  (41.4%) to  $E=Sn$  (55.1%), but decreases when  $E=$ Pb (51.7%).

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- [1] a) G. N. Lewis, J. Am. Chem. Soc. 1916, 38, 762; b) G. N. Lewis, Valence and the Structure of Atoms and Molecules, American Chemical Society Monograph Series, New York, 1923.
- [2] According to Mierzecki, the conception of the covalent bond was introduced by William Ramsey: R. Mierzecki, The Historical Development of Chemical Concepts, Kluwer Academic Publishers, Dordrecht, 1985, p. 202. Lewis writes in his publication (ref. [1a]) that William Ramsay used very similar formulae to his in the book: The Temple Primers; Modern Chemistry.
- [3] We wish to point out that the accumulation of electronic charge in the bonding region is a result of chemical interactions but not the driving force. Also, as one referee pointed out, covalent interactions do not necessarily lead to an accumulation of the electronic charge

in the bonding region. An example is the chemical bond in  $F<sub>2</sub>$ . The Laplacian distribution of the electron density shows depletion of electronic charge in the bonding region of  $F_2$ . This was discussed by Cremer and Kraka who suggested that the energy density at the bond's critical point should be used as a sensitive probe for covalent bonding: D. Cremer, E. Kraka, Angew. Chem. 1984, 96, 612; Angew. Chem. Int. Ed. Engl. 1984, 23, 62. It is evident that energy is a more direct criterion for chemical bonding than charge distribution. Schwarz et al. have shown that an accumulation of electronic charge in the bonding region of  $F<sub>2</sub>$  is found when the differences between the electron density of  $F_2$  and the properly arranged fluorine atoms is calculated: W. H. E. Schwarz, L. Mensching, K. Ruedenberg, L. L. Miller, P. Valtazanos, W. von Niessen, R. A. Jacobson, Angew. Chem. 1989, 101, 605; Angew. Chem. Int. Ed. Engl. 1989, 28, 597.

- [4] W. Heitler, F. London, Z. Phys. **1927**, 44, 455.
- [5] The attractive part of the (covalent or ionic) chemical bonding results from the electrostatic forces derived from a nuclear–electron attraction. The counterpart of the electrostatic interactions is the kinetic energy. The kinetic energy, at the equilibrium distance, has a repulsive contribution whose absolute value is, according to the virial theorem, half the electrostatic attraction. This is discussed in refs. [6,10,11,13]. Our work focuses on and distinguishes between the electrostatic attraction, which is given by the quasiclassical term  $\Delta E_{\text{elstat}}$ , and the orbital interaction (resonance) term,  $\Delta E_{\text{orb}}$ .
- [6] A thorough discussion of previous work and the present understanding of the chemical bonding is given by: W. Kutzelnigg in The Concept of the Chemical Bond (Ed.: Z. B. Maksic), Springer, Berlin/Heidelberg, 1990.
- [7] The term "quasiclassical" is used to indicate that the electron density  $\rho$  is calculated by using quantum theory but the interactions between the electrons and nuclei are calculated by assuming classical behaviour, that is, that no quantum interference takes place.
- [8] M. A. Spackman, E. N. Maslen, J. Phys. Chem. 1986, 90, 2020.
- [9] K. P. Huber, G. Herzberg, Molecular Spectra and Molecular Structure IV. Constants of Diatomic Molecules, Van Nostrand-Reinhold, New York, 1979.
- [10] F. L. Hirshfeld, S. Rzotkiewicz, Mol. Phys. 1974, 27, 1319.
- [11] a) S. G. Wang, W. H. E. Schwarz, H. L. Lin, Chem. Phys. Lett. 1991, 180, 509; b) J. Autschbach, W. H. E. Schwarz, J. Phys. Chem. A 2000, 104, 6039.
- [12] a) F. M. Bickelhaupt, E. J. Baerends, Rev. Comput. Chem. 2000, 15, 1; b) G. te Velde, F. M. Bickelhaupt, E. J. Baerends, S. J.A. van Gisbergen, C. Fonseca Guerra, J. G. Snijders, T. Ziegler, J. Comput. Chem. 2001, 22, 931.
- [13] F. Rioux, Chem. Educ. **2003**, 8, 1.
- [14] K. Ruedenberg, Rev. Mod. Phys. 1962, 34, 326.
- [15] L. Pauling, The Nature of the Chemical Bond, 3rd ed., Cornell University Press, Ithaca, New York, 1960.
- [16] a) J. E. Lennard-Jones, *Trans. Faraday Soc.* **1929**, 25, 668; b) E. Hückel, Z. Phys. 1931, 70, 204.
- [17] R. B. Woodward, R. Hoffmann, The Conservation of Orbital Symmetry, Verlag Chemie, Weinheim, 1970.
- [18] C. Massera, G. Frenking, unpublished results.
- [19] K. Morokuma, J. Chem. Phys. **1971**, 55, 1236.
- [20] a) T. Ziegler, A. Rauk, Inorg. Chem. 1979 18, 1558; b) T. Ziegler, A. Rauk, Inorg. Chem. 1979, 18, 1755.
- [21] a) O. Gritsenko, P. Schipper, E. J. Baerends, J. Chem. Phys. 1997, 107, 5007; b) E. J. Baerends, O. Gritsenko, J. Phys. Chem. A 1997, 101, 5383; c) D. Chong, O. Gritsenko, E. J. Baerends, J. Chem. Phys. 2002, 116, 1760.
- [22] a) A. Diefenbach, F. M. Bickelhaupt, G. Frenking, J. Am. Chem. Soc. 2000, 122, 6449; b) J. Uddin, G. Frenking, J. Am. Chem. Soc. 2001, 123, 1683; c) Y. Chen, G. Frenking, J. Chem. Soc., Dalton Trans. 2001, 434; d) M. Lein, J. Frunzke, A. Timoshkin, G. Frenking, Chem. Eur. J. 2001, 7, 4155; e) M. Doerr, G. Frenking, Z. Allg. Anorg. Chem. 2002, 628, 843; f) G. Frenking, K. Wichmann, N. Fröhlich, J. Grobe, W. Golla, D. Le Van, B. Krebs, M. Läge, Organometallics 2002, 21, 2921; g) J. Frunzke, M. Lein, G. Frenking, Organometallics 2002, 21, 3351; h) C. Loschen, K. Voigt, J. Frunzke, A. Diefenbach,

M. Diedenhofen, G. Frenking, Z. Allg. Anorg. Chem. 2002, 628, 1294; i) V. M. Rayón, G. Frenking, Chem. Eur. J. 2002, 8, 4693; j) M. Cases, G. Frenking, M. Duran, M. Solà, Organometallics 2002, 21, 4182; k) C. Esterhuysen, G. Frenking, Theor. Chim. Acta 2004, 111, 381; l) M. Lein, A. Szabó, A. Kovács, G. Frenking, Faraday Discuss. 2003, 124, 365; m) C. Esterhuysen, G. Frenking, Chem. Eur. J. 2003, 9, 3518; n) G. Frenking, K. Wichmann, N. Fröhlich, C. Loschen, M. Lein, J. Frunzke, V. M. Rayón, Coord. Chem. Rev. 2003, 238/239, 55.

- [23] a) F. M. Bickelhaupt, U. Radius, A. W. Ehlers, R. Hoffmann, E. J. Baerends, New J. Chem. 1998, 22, 1; b) U. Radius, F. M. Bickelhaupt, A. W. Ehlers, N. Goldberg, R. Hoffmann, Inorg. Chem. 1998, 37, 1080; c) A. W. Ehlers, E. J. Baerends, F. M. Bickelhaupt, U. Radius, Chem. Eur. J. 1998, 4, 210; d) A.A. Dickinson, D. J. Willock, R. J. Calder, S. Aldridge, Organometallics 2002, 21, 1146; e) L. E. Forslund, N. Kaltsoyannis, New J. Chem. 2003, 27, 1108.
- [24] a) A. D. Becke, Phys. Rev. A 1988, 38, 3098; b) J. P. Perdew, Phys. Rev. B 1986, 33, 8822.
- [25] a) J. G. Snijders, E. J. Baerends, P. Vernooijs, At. Nucl. Data Tables 1982, 26, 483; b) J. Krijn, E. J. Baerends, Fit Functions in the HFS-Method, Internal Report (in Dutch), Vrije Universiteit Amsterdam, The Netherlands, 1984.
- [26] a) C. Chang, M. Pelissier, Ph. Durand, Phys. Scr. 1986, 34, 394; b) J.-L. Heully, I. Lindgren, E. Lindroth, S. Lundquist, A.-M. Martensson-Pendrill, J. Phys. B 1986, 19, 2799; c) E. van Lenthe, E. J. Baerends, J. G. Snijders, J. Chem. Phys. 1993, 99, 4597; d) E. van Lenthe, E. J. Baerends, J. G. Snijders, J. Chem. Phys. 1996, 105, 6505; e) E. van Lenthe, R. van Leeuwen, E. J. Baerends, J. G. Snijders, Int. J. Quantum Chem. 1996, 57, 281.
- [27] E. L. Hirshfeld, Theor. Chim. Acta 1977, 44, 129.
- [28] The preparation energy may also include electronic excitation energy if the electronic ground state of the fragment is different from the electronic reference state in the molecule. For example, the electronic reference state of the CH fragment in acetylene,  $HC =$ CH, is the  $(^{4}\Sigma^{-})$  quartet state but the electronic ground state is  $^{2}\Pi$ .
- [29] F. M. Bickelhaupt, N. M. M. Nibbering, E. M. van Wezenbeek, E. J. Baerends, J. Phys. Chem. 1992, 96, 4864.
- [30] The EPA calculation of H<sub>2</sub> at the BP86/TZ2P level gives  $\Delta E_{orb}$ =  $-99.6$  kcalmol<sup>-1</sup> and  $\Delta E_{\text{Pauli}} = -19.1$  kcalmol<sup>-1</sup>. The latter value is an artefact of the density functionals that were used. It is reasonable to add the unphysical  $\Delta E_{\text{Pauli}}$  value to the orbital interaction term: F. M. Bickelhaupt, personal communication.
- [31] See ref. [6], p. 34.
- [32] See ref. [12a], p. 15.
- [33] W. Kutzelnigg, Angew. Chem. 1984, 96, 262; Angew. Chem. Int. Ed. Engl. 1984, 23, 272.

Chem. Eur. J. 2005, 11, 1813–1825 <www.chemeurj.org> © 2005 Wiley-VCH Verlag GmbH & Co. KGaA, Weinheim 1825

- [34] See ref. [6], p. 35.
- [35] CRC Handbook of Chemistry and Physics, 81st ed. (Ed.: D.R. Lide), CRC Press, Boca Raton, 2000, pp. 9-17 (geom.) and 9-55 (diss. energy).
- [36] J. W. Ochterski, G. A. Petersson, K. B. Wiberg, J. Am. Chem. Soc. 1995, 117, 11 299.
- [37] P. J. Bruna, G. A. Di Labio, J. S. Wright, *J. Phys. Chem.* **1992**, *96*, 6269.
- [38] I. Demachy, F. Volatron, J. Phys. Chem. 1994, 98, 10728.
- [39] J. Koput, J. Mol. Spectrosc. 1986, 115, 438.
- [40] R. F. W. Bader, Atoms in Molecules. A Quantum Theory, Clarendon Press, Oxford, 1990.
- [41] M. Lein, G. Frenking in Theory and Applications of Computational Chemistry: The First 40 Years (Eds.: C. E. Dykstra, K. S. Kim, G. Frenking, G. E. Scuseria), Elsevier, Amsterdam, in press.
- [42] D. F. McMillen, D. M. Golden, Ann. Pharm. Belg. Ann. Rev. Phys. Chem. 1982, 33, 493.
- [43] a) J. L. Lyman, *J. Phys. Chem. Ref. Data*, **1989**, 18, 799; b) J. Berkowitz, P. M. Dehmer, W. A. Chupka, J. Chem. Phys. 1973, 59, 925.
- [44] D. D. Danielson, J.V. Patton, K. Hedberg, J. Am. Chem. Soc. 1977, 99, 6484.
- [45] M. M. Gilbert, G. Gundersen, K. Hedberg, J. Chem. Phys. 1972, 56, 1691.
- [46] R. H. Jackson, J. Chem. Soc. 1962, 4585.
- [47] C. R. Brundle, M. B. Robin, N. A. Kuebler, H. Basch, J. Am. Chem. Soc. 1972, 94, 1451.
- [48] The correlation between hybridization and electronegativity is known as Bent's rule: H. A. Bent, Chem. Rev. 1961, 61, 275.
- [49] J. R. Durig, Z. Shen, J. Phys. Chem. A 1997, 101, 5010.
- [50] A. P. Rendell, T. J. Lee, *J. Chem. Phys.* **1994**, 101, 400.
- [51] M. Peric, B. Ostojic, B. Engels, J. Mol. Spectrosc. 1997, 182, 295.
- [52] B. Ruscic, J. Berkowitz, J. Chem. Phys. 1991, 95, 4378.
- [53] C. Jouany, J. C. Barthelat, J. P. Daudey, Chem. Phys. Lett. 1987, 136, 52.
- [54] J. Demaison, F. Hegelund, H. Burger, J. Mol. Struct. 1997, 413, 447.
- [55] M. Kaupp, B. Metz, H. Stoll, Angew. Chem. 2000, 112, 4780; Angew. Chem. Int. Ed. 2000, 39, 4607.
- [56] A. Ricca, C. W. Bauschlicher, Jr., J. Phys. Chem. A 1999, 103, 11 121.
- [57] P. von R. Schleyer, M. Kaupp, F. Hampel, M. Bremer, K. Mislow, J. Am. Chem. Soc. 1992, 114, 6791.
- [58] P. Pyykkö, Chem. Rev. 1988, 88, 563.

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